A status update on the **neutrino mechanism of core-collapse supernovae**

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Introduction:

What questions do we aim to answer? The core-collapse puzzle and its history.

Physical Processes:

Core collapse. The stalled shock and its revival.

The Delayed-Neutrino Mechanism: The status of current simulations.

THE Status OF CUITERT SITUATION

Alternative Ideas:

Jets / nuclear burning / GR / MHD?

Pulsar Kicks:

Recoil from core-collapse explosions.

Collaborators: T. Brandt (IAS), M. Rantsiou (MPA), C. Ott (Caltech), E. Livne (Hebrew Univ.), A. Almgren (LBL), J. Bell (LBL), A. Burrows (Princeton), O. Papish (Technion), N. Soker (Technion)





"Every passing hour brings the Solar System 43,000 miles closer to Globular Cluster MI3 in Hercules - and still there are some misfits who insist there is no such thing as progress" - Ransom K. Fern

> Kurt Vonnegut The Sirens Of Titan

Progenitors: Massive stars $8-50 M_{\odot}$

Energies:Neutron star binding energy: $\sim 3 \times 10^{53}$ ergKinetic energy of ejecta: $\sim 10^{51}$ ergLight-curve energy: $\sim 10^{49}$ erg

Timescales:

Core collapse: Post-bounce time to explosion: Core neutrino cooling time:

 $\sim 500 \text{ ms}$ $\leq 1 \text{ s}$ $\sim 10 \text{ s}$

Products: Blast wave, heavy-elements, compact object remnants.

I. Canonical explosion energy of I Bethe.

2. Neutron star mass distribution.

3. Nucleosynthetic yields and distributions.

4. Pulsar Kicks.

What physics is necessary?



Potentially Important Ingredients

- Gravity
- Neutrino Heating
- Turbulence/Convection and Shock Instabilities
- Rotation
- Magnetic fields
- Nucleosynthesis
- General Relativity

Multi-dimensional effects important!

Goal: 3D models with sufficient realism that produce canonical SN explosions

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Electron capture, nuclear dissociation initiate dynamical collapse. Collapse halted at nuclear densities, shock wave forms as core matter is suddenly decelerated.

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Early simulations: Bounce shock stalls at ~100 - 200 km. Sapped of pressure by electron capture, neutrino losses.

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Lower densities implies neutrinos are less trapped: $\rho \sim 10^{13} \text{ g cm}^{-3}$ Burst of flux over ~100 ms, radiation pressure ejects envelope?

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3D simulations (2010 -):

Detailed neutrino transport Some weak explosions. MHD, GR, other secondary physics. No realistic simulation has produced a supernova with canonical energy.



Massive iron core electrons become relativistically degenerate.

Adiabatic exponent of $\gamma \leq \frac{4}{3}$ implies unstable to dynamical collapse.

Collapse halted when equation of state stiffens due to nucleons.

Inner core:

Remins in sonic contact, rebounds as a unit.

Bounce dissociates nuclei.

Outer material accretes supersonically, hits "wall" to produce a bounce shock.



Neutrino-matter interactions

Trapped electron neutrinos create a degenerate Fermi sea.

Stimulated absorption in reactions due to Pauli blocking (stimulated *emission* for photons).

Neutrino Types:

Electron u_e Muon u_μ Tau $u_ au$

Typical Energies:

Beta Decay Neutrinos Solar Neutrinos Supernova Neutrinos

 $\leq 0.5 \text{ MeV}$ $\sim 0.1 - 17 \text{ MeV}$ $\sim 5 - 40 \text{ MeV}$

 $\bar{\nu}_{\mathrm{e}}$

 $ar{
u}_{\mu} \ ar{
u}_{ au}$

Anti-Electron

Anti-Muon

Anti-Tau





Neutrino-matter cross sections are very low.

Thomson electron scattering cross section: $\sim 10^{-24}~{
m cm}^2$

Weak interaction cross sections for supernova energies: $\sim 10^{-42} \text{ cm}^2$ Mean free path $\sim 100 \left(\frac{10^{15} \text{ g cm}^{-3}}{\rho}\right) \left(\frac{10 \text{ MeV}}{\epsilon_{\nu}}\right)^2 \text{ cm}$

Significant interactions:

Reaction	Neutrino Type	Cross Section $\sigma \left[\times 10^{-42} \text{cm}^2 \right]$
$\nu_e + n \longleftrightarrow e^- + p$	Electron	$\sim 8 \left(\frac{\epsilon_{\nu}}{10 \text{ MeV}}\right)^2$
$\bar{\nu_e} + p \longleftrightarrow n + e^+$	Anti-electron	$\sim 7 \left(\frac{\epsilon_{\nu}}{10 \text{ MeV}}\right)^2$
$\nu_i + p \longrightarrow \nu_i + p$	All species	$\sim 1.7 \left(\frac{\epsilon_{\nu}}{10 \text{ MeV}}\right)^2$
$\nu_i + n \longrightarrow \nu_i + n$	All species	$\sim 2.0 \left(\frac{\epsilon_{\nu}}{10 \text{ MeV}}\right)^2$
$\nu_i + A \longrightarrow \nu_i + A$	All species	$\sim 1.2 \left(\frac{\epsilon_{\nu}}{10 \text{ MeV}}\right)^2$
$\nu_i + e^- \longrightarrow \nu_i + e^-$	All species	$ \nu_e : \sim 5 \left(\frac{\epsilon_{\nu}}{10 \text{ MeV}} \right) \left(\frac{T + \mu_e/4}{10 \text{ MeV}} \right) $

Shock wave propagates into heavy nuclei with high specific heat.

Shock energy goes into:
electron capture $A + e^- \rightarrow A' + \nu_e$ nuclear dissociation ${}^{56}_{26}\text{Fe} \rightarrow 26p + 30n$ Post-shock pressure fallsRam pressure $p_{ram} = \rho v^2$ may be more
than post shock pressure

Prompt explosion will only work if ram pressure drops.

Requires a steep density gradient. $8-10 M_{\odot}$

Otherwise $p_{\rm ram} > p_{\rm post-shock}$ implies that the shock stalls.



Need to either increase increase $p_{\mathrm{post-shock}}$, decrease p_{ram} , or both by:

Depositing additional energy behind the shock

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Using progenitor models with steeper density profiles (no).

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m ram}$, or both by:

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Possible energy sources:

Nuclear burning (O into Fe).

Releases ~ $5 \times 10^{17} \text{ erg g}^{-1} \ll 10^{19} \text{ erg g}^{-1} \sim U_{\text{grav,be}}(r = 200 \text{ km})$ For 10^{51} erg need to burn $1M_{\odot}$ of oxygen explosively, implies need to already have enormous blast wave at large radii. See Kushnir 2015.

Annihilation: $\nu_e + \bar{\nu}_e \to e^+ + e^- \to 2\gamma$

Most efficient where neutrino-cooling is severe

Delayed neutrino heating: the neutrino mechanism.

Simplified neutrino radiation transport, neglecting scattering:

$$\frac{\partial I_{\epsilon}(r)}{\partial r} = \kappa_{\epsilon} \rho [B_{\epsilon}(T) - I_{\epsilon}(r)]$$

$$B_{\epsilon}(T) \text{ is the neutrino blackbody function.}$$

Integrated over
$$\epsilon_{\nu}$$
: $\frac{\partial F(r)}{\partial r} = \bar{\kappa}\rho[acT^4 - F(r)]$

 $\bar{\kappa}\rho acT^4$ is emission from matter (cooling).

 $\bar{\kappa}\rho F(r)$ is absorption by matter (heating).

Neutrino cooling dominated by URCA processes:

Electron capture: $p + e^- \rightarrow \nu_e + n$

Positron capture: $n + e^+ \rightarrow \bar{\nu}_e + p$

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Neutrino energy loss rate per gram: $\bar{\kappa}acT^4$ $\bar{\kappa} \propto \epsilon_{\nu}^2 \Rightarrow \bar{\kappa} \propto T^2$ Cooling rate per gram: $\mathcal{C} \approx 1.4 \times 10^{20} \left(\frac{T}{2 \text{ MeV}}\right)^6 \text{ erg g}^{-1} \text{ s}^{-1}$

Cooling dominates at R < 80 km where matter is hot.

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u}$

Neutrino capture, inverses of URCA processes:

$$\bar{\nu_e} + p \to n + e^+$$

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$$\overline{\nu_e} + p \to n + e^+ \\
\nu_e + n \to p + e^- \\
\overline{\kappa} \propto \epsilon_{\nu}^2 \Rightarrow \overline{\kappa} \propto T_{\nu_e}^2 \\
\text{Heating rate per gram:} \quad \mathcal{H} \propto T_{\nu_e}^2 \frac{L_{\nu}}{4\pi r^2} \\
\mathcal{H} \approx 1.5 \times 10^{20} L_{\nu_e} \left(\frac{100 \text{ km}}{r}\right)^2 \left(\frac{T_{\nu_e}}{4 \text{ MeV}}\right)^2 \text{ erg g}^{-1} \text{ s}^{-1}$$

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Gain region: Net neutrino heating

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Gain Region



Gain region: Net neutrino heating $\mathcal{H} - \mathcal{C} > 0 \Rightarrow 80 \text{ km} - R_{\text{shock}}$

Net neutrino heating adds $\sim 10^{20} \ {\rm erg \ g^{-1} \ s^{-1}}$ to the gain region.

Matter gains sufficient energy to become unbound in ~ 100 ms.

Quantity	Definition	Description
Residence Time	$ au_{ m res}$	Mean dwell time in the gain region.
HeatingTime	$ au_{\mathbf{q}} \equiv rac{\int_{\mathrm{gain}} U_{\mathrm{int}}}{\int_{\mathrm{gain}} (\mathcal{H} - \mathcal{C})}$	Characteristic timescale to heat gain region.
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If sustained, shock is revived.			
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To make neutrino mechanism work, need to increase $\, au_{
m res}\,$ and/or $L_
u$.

Convection and GR: Increasing $\mathcal{P} \equiv \tau L_{\nu}$

Core convection can dredge up trapped neutrinos, potentially increasing the neutrino luminosities.

Not seen in high-res multi-D simulations.

Outer core convection only.



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General Relativity

Relativity tends to make the core more compact.

Hotter neutrino-spheres imply higher cross-sections which imply more heating. But neutrinos are redshifted from the deeper well...

GR effects seem to give minor corrections to P.



Multidimensional Effects: Increasing au_{res}

Enormous computing power: Fully 3D simulations.

Fundamentally different results in spherically symmetric, axisymmetric, 3D simulations.

Dynamics different.

Dwell times different.

Turbulence different.



CASTRO: Compressible Astrophysics

- Multi-D radiation-hydrodynamics code
- Adaptive mesh refinement (AMR) with sub-cycling in time
- Advection: 2nd order, unsplit piecewise-linear or PPM
- Radiation: multi-group flux limited diffusion
- Gravity: Monopole or multi-grid Poisson solve
- Scales to over 200,000 cores!

Ann Almgren (LBL) John Bell (LBL) Louis Howell (LLNL)



3D AMR block structure

Non-Rotating Initial Model

Time=0.144418 s



2000 kilometers



Standing Accretion Shock Instability (SASI)

Axisymmetric

 $\ell = 1 \mod \ell$ is dominant

Suggested as a fundamental characteristic of SN dynamics and way to spin-up pulsars;

Blondin & Mezzacappa 2007



2000 kilometers



Dimensional Dependence

Spherically Symmetric

Axisymmetric



Nordhaus et al. 2010

Dimensional Dependence

Axisymmetric

Three Dimensional



Nordhaus et al. 2010





Multidimensional Effects: Increasing au_{res}



Critical curve for explosions



<u>3D explodes earlier</u>

Nordhaus et al. 2010 Dolence et al. 2014 Burrows et al. 2013 Hanke et al. 2012

2D and 3D explode same time

Hanke et al. 2012 Melson et al. 2014

2D explodes earlier

Couch 2014 Couch & O'Connor 2013 Takiwaki al. 2014

Controversial - different groups, different codes, different results.

All 3D simulations to date:

if explosion, under-energetic by factors of 10-100.

Inherent limitation of the neutrino-mechanism?

Under the most extremely favorable conditions, neutrinos may accelerate the gas to energy of 5e50 erg.

Papish, Nordhaus, Soker 2015 MNRAS

General relativistic effects: to date mostly 2D and conformally flat.

MHD: linear winding and compression only.

Nucleosynthesis: if neutrinos fail, perhaps nuclear burning. Kushnir 2015

Jets, winds: angular momentum present, jets ubiquitous in astrophysics.

see Jittering-Jet model/papers of Oded Papish

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Neutron Star Kicks



Nordhaus et al. 2010b



Neutron Star Kicks

Pulsar birth velocities typically 300 - 400 $~{\rm km~s^{-1}}$

Explosion primarily in +Z direction...

...leads to NS recoil in -Z direction

Hydrodynamic Origin of Pulsar Kicks



Nordhaus et al. 2010b

Radiation field is smooth... ... matter field is not.

Flux Vectors $\Omega = 0$ Entropy \mathcal{V}_{e} Time = -194.5 ms21.01 MeV Distance = 500.0 km

CASTRO - with neutrino heating/cooling scheme



Hydrodynamic Origin of Pulsar Kicks





Pulsar Kicks

Gravitational effects are important.

With AMR can follow evolution farther in time.

NS decoupled from surroundings



At late times, gravity of the slow-moving ejecta dominates.





Takeaways

State-of-the-art neutrino-driven core-collapse simulations do not reach supernova energies when they explode.

Inherent limitation of the neutrino-mechanism: Papish, Nordhaus, Soker 2015.

Alternate theories/processes needed: GR, MHD, nuclear burning.

Pulsar kicks are a hydrodynamic outcome of explosions.

