# 1016-345-01 <br> Probability and Statistics for Engineers 

## Problem Set 7

Assigned 2012 October 23
Due 2012 October 30

Show your work on all problems! If you use a computer to assist with numerical computations, turn in your source code as well.

## 1 Devore Chapter 5, Problem 38

Note that problem 5.38 is different in the seventh and eighth editions of Devore. Be sure to do the problem from the eighth edition.

## 2 Devore Chapter 5, Problem 46

## 3 Devore Chapter 5, Problem 50

## 4 Devore Chapter 5, Problem 66

## 5 Computational Exercise (Extra Credit)

A random variable $X$ obeying a $\chi^{2}$ distribution with $\nu$ degrees of freedom has a pdf

$$
f(x ; \nu)= \begin{cases}\frac{1}{2^{\nu / 2} \Gamma(\nu / 2)} x^{(\nu / 2)-1} e^{-x / 2} & x>0  \tag{5.1}\\ 0 & x<0\end{cases}
$$

as well as a mean $\mu=\nu$ and variance $\sigma^{2}=2 \nu$. Since it is the sum of $\nu$ iid rvs (each of which is the square of a standard normal random variable), the central limit theorem says that it should be approximated, in the limit that $\nu$ is large, by a normal distribution

$$
\begin{equation*}
f(x ; \nu) \approx f(x)=\frac{1}{\sigma \sqrt{2 \pi}} e^{-(x-\mu)^{2} /\left(2 \sigma^{2}\right)} \tag{5.2}
\end{equation*}
$$

a. For $0<x<20$, plot the exact chi-squared pdf and the normal approximation for $\nu=5$.
b. For $0<x<200$, plot the exact chi-squared pdf and the normal approximation for $\nu=50$.

Warning: If you use matplotlib via
ipython -pylab
the gamma imported into your namespace produces gamma-distributed random variables; if you want the gamma function to calculate $\Gamma(\nu / 2)$ you'll need
from scipy.special import gamma

