

1016-345-01  
Probability and Statistics for Engineers

Problem Set 1

Assigned 2013 March 5  
Due 2013 March 12

**Show your work on all problems!**

**1 Devore Chapter 2, Problem 14**

*Note that problem 2.14 is different in the seventh and eighth editions of Devore. Be sure to do the problem from the eighth edition.*

**2 Devore Chapter 2, Problem 34**

*Note that problem 2.34 is different in the seventh and eighth editions of Devore. Be sure to do the problem from the eighth edition.*

**3 Devore Chapter 2, Problem 60**

**4 Devore Chapter 2, Problem 110**

**5 Computational Exercise (Extra Credit)**

This exercise lets you see how the relative frequency an outcomes in a repeated experiment approximates the probability of that outcome.

Generate a sequence of  $N = 1,000,000$  random integers, each equally likely to be 1, 2, 3, 4, or 5. Define  $n_k$  to be the number of fives in the first  $k$  integers in your sequence, so that  $n_k/k$  is the relative frequency of fives among the first  $k$  integers. By the definition of probability as a limiting relative frequency,  $\lim_{k \rightarrow \infty} \frac{n_k}{k} = \frac{1}{5} = .2$

- Plot  $\frac{n_k}{k}$  versus  $k$  for  $1 \leq k \leq 50$ .
- Plot  $\frac{n_k}{k}$  versus  $k$  for  $1 \leq k \leq 1000$ .
- Produce a semilog plot of  $\frac{n_k}{k}$  versus  $k$ , using a logarithmic scale for  $1 \leq k \leq 10^6$ .

*Hint:* if you use matlab or the python library NumPy for your calculations, you may find the `cumsum()` function useful, along with the construction `d==5`, which will produce an array of true (1) and false (0) values of the same size as `d`.