

Probability and Statistics for Engineers

Problem Set 7

Assigned 2013 April 23
Due 2013 April 30

Show your work on all problems! If you use a computer to assist with numerical computations, turn in your source code as well.

1 Devore Chapter 5, Problem 38

Note that problem 5.38 is different in the seventh and eighth editions of Devore. Be sure to do the problem from the eighth edition.

2 Devore Chapter 5, Problem 46**3 Devore Chapter 5, Problem 50****4 Devore Chapter 5, Problem 66****5 Computational Exercise (Extra Credit)**

A random variable X obeying a χ^2 distribution with ν degrees of freedom has a pdf

$$f(x; \nu) = \begin{cases} \frac{1}{2^{\nu/2}\Gamma(\nu/2)} x^{(\nu/2)-1} e^{-x/2} & x > 0 \\ 0 & x < 0 \end{cases} \quad (5.1)$$

as well as a mean $\mu = \nu$ and variance $\sigma^2 = 2\nu$. Since it is the sum of ν iid rvs (each of which is the square of a standard normal random variable), the central limit theorem says that it should be approximated, in the limit that ν is large, by a normal distribution

$$f(x; \nu) \approx f(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-(x-\mu)^2/(2\sigma^2)} \quad (5.2)$$

- a. For $0 < x < 20$, plot the exact chi-squared pdf and the normal approximation for $\nu = 5$.
- b. For $0 < x < 200$, plot the exact chi-squared pdf and the normal approximation for $\nu = 50$.

Warning: If you use matplotlib via

```
ipython --pylab
```

the `gamma` imported into your namespace produces gamma-distributed random variables; if you want the gamma function to calculate $\Gamma(\nu/2)$ you'll need

```
from scipy.special import gamma
```