MATH 252-01: Probability and Statistics II

Problem Set 4

Assigned 2018 February 6 Due 2018 February 13

Show your work on all problems! If you use a computer to assist with numerical computations, turn in your source code as well.

1 Devore Chapter 8, Problem 36

Note that problem 8.36 is different in the eighth and ninth editions of Devore. Be sure to do the problem from the ninth edition.

2 Devore Chapter 8, Problem 50

Note that problem 8.50 is different in the eighth and ninth editions of Devore. Be sure to do the problem from the ninth edition.

3 Devore Chapter 8, Problem 70

Note that problem 8.70 is different in the eighth and ninth editions of Devore. Be sure to do the problem from the ninth edition.

4 Computational Exercise

Download the following data set which is a sample of size n = 30 from a normal distribution with unknown σ :

http://ccrg.rit.edu/~whelan/courses/2018_1sp_MATH_252/data/ps04_prob4.dat using the username and password given in class.

- a. Consider the null hypothesis $H_0: \mu = 0$ and the alternative hypothesis $H_a: \mu \neq 0$. Carry out the appropriate test at 90% confidence level, and indicate whether you would reject H_0 in favor of H_a . If you use a software package like minitab which performs the test for you, explain the meaning of each of the quantities it outputs.
- **b.** Your results from part (a) should contain the quantities needed to construct the test statistic by hand. Explicitly combine them and compare to the percentiles of the t distribution appropriate for this sample size, and to the standard normal distribution. Comment on the appropriateness of the large sample approximation in this case.
- **c.** Now change the alternative hypothesis to $H_a': \mu > 0$ and repeat the test.
- **d.** Return to the original alternative hypothesis $H_a: \mu \neq 0$, and now assume that the population standard deviation is known to be $\sigma = 5$. Carry out the appropriate test in this case.